

# FORECASTING OF TRAFFIC JAMS CAUSED BY ADVERSE WEATHER

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# Objectives

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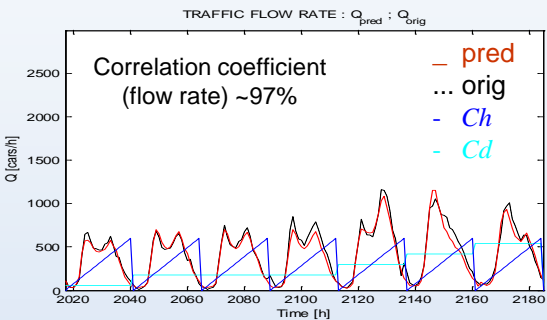
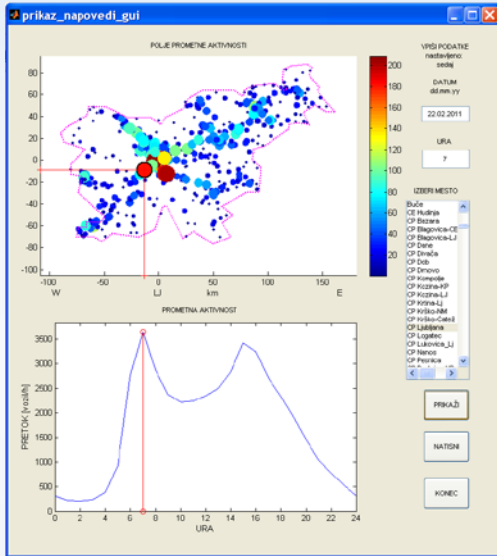
- **Problem:** How to forecast formation and characteristics of traffic jams caused by adverse weather?
- **Example:** Evolution of traffic jam on road section with increased slipperiness or fog.
- **Source of information:** Forecasted traffic flow at critical road sector and appropriate speed limit determined from road weather conditions.
- **Mathematical tool:** Hybrid system comprised of: input traffic flow, road capacity and jam estimators.
- **Goal:** To develop an intelligent unit for traffic information providers and road operators.





### Prediction of traffic flow rate (normal driving conditions)

Basis: Prediction is performed by a non-parametric statistical model using previously recorded time series of flow rate.



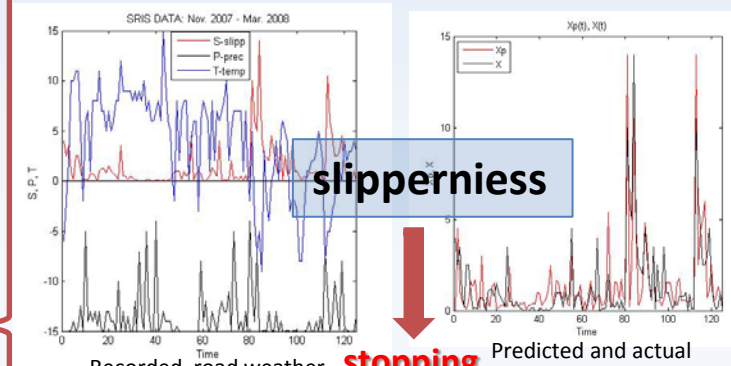
### Prediction of traffic jam

Intelligent unit Basis: Hybrid system comprised of: input traffic flow, road capacity and jam estimators



### Prediction of road weather conditions

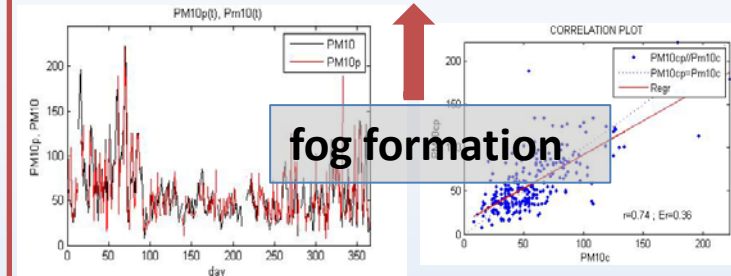
Basis: Prediction is performed by a non-parametric statistical model using previously recorded road weather data.



slippiness

stopping distance

$$X_{st} = X_{react} + X_{break}$$



fog formation

The fog formation is predicted from previous records of: concentration of particulate matter PM10, wind velocity W, humidity H and temperature T



# Estimation of speed limit

- A proper speed limit on wet road is obtained by equalizing stopping distances at normal and wet conditions:

$$X_{st1} = X_{st2} - \text{black arrow}$$

Due to decay of  $\mu(v)$  the stopping distance is increased:

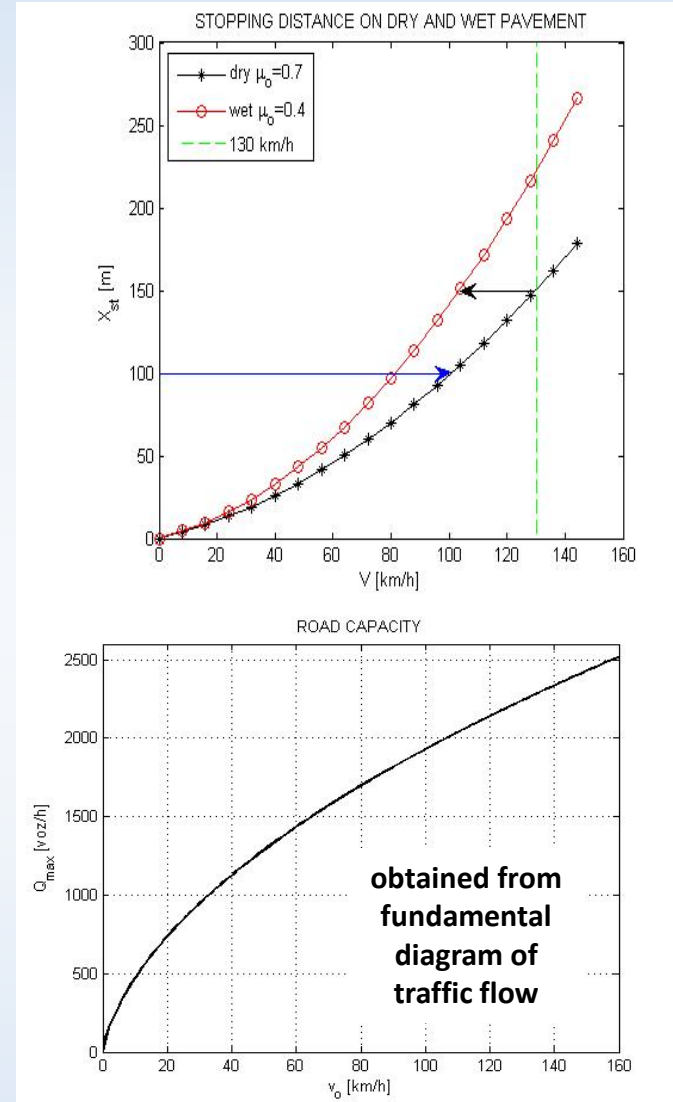
$$X_{st} = X_{react} + X_{break} \approx \tau v + \exp(0.7v/c) v^2/2 \mu_o g$$

- A proper speed limit at decreased visibility is obtained by equalizing stopping and visibility distance:

$$X_{st2} = X_{vis} - \text{blue arrow}$$

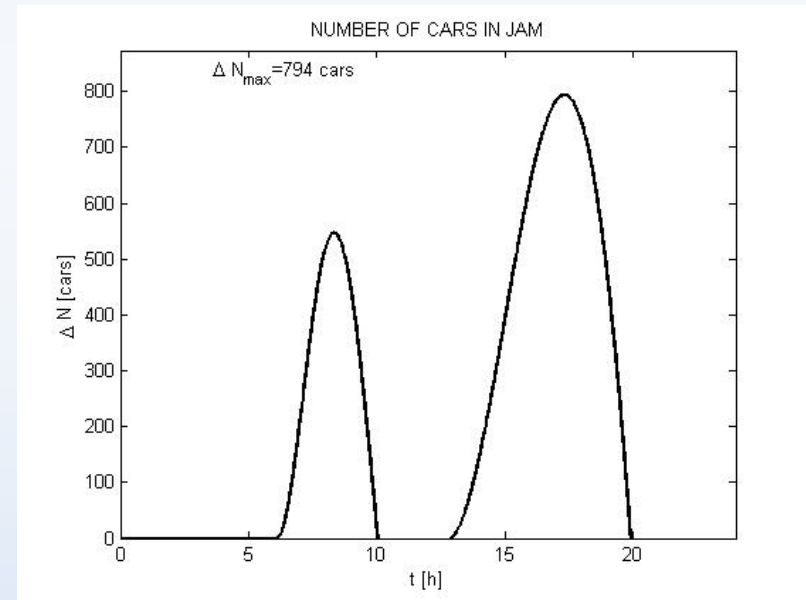
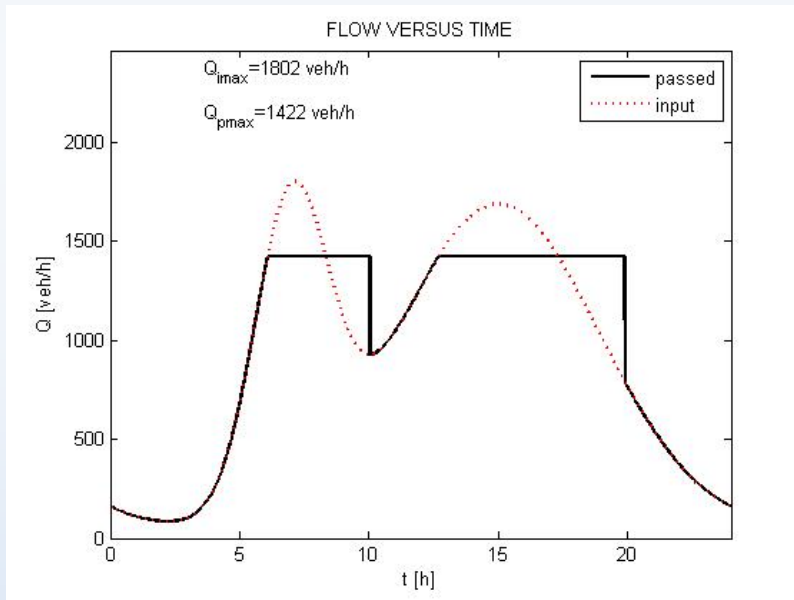
**Speed limit determines the road capacity**

***Q<sub>max</sub>.***



# Estimation of jam length

- When the input flow surpasses the road capacity:  $Q_{in} > Q_{max}$ , a jam starts to evolve.
- The number of cars in jam is estimated by the integral:  $\Delta N = \int (Q_{in} - Q_{max}) dt$ .
- The time that a car coming to the jam spends to pass it is estimated by:  $T_J = \Delta N / Q_{max}$ .
- The jam length can be estimated by this time and velocity of the car:  $L = T_J * v_c$





# Determination of traffic jam characteristics

## Description by field equations

- Velocity adaptation law:

- $$\frac{\partial v}{\partial t} + v \frac{\partial v}{\partial x} = \frac{v_e(\rho) - v}{T};$$

- Relaxation time:  $T \cong 3\tau$

- Continuity equation:

- $$\frac{\partial \rho}{\partial t} + \frac{\partial \rho v}{\partial x} = I(x, t)$$

- Traffic source term:

- $$I(x, t) = Q(t)\delta(x, t) \quad ; \quad Q(t) \text{ is forecast}$$

## Numerical treatment

- Cell dimensions:  $\Delta x = \lambda$  ;  $\Delta t = 0.1\tau$

- Intervals:  $0 < x < 0.5\text{km}$  ;  $0 < t < 1\text{h}$

- Initial and boundary conditions:

- $$\rho = 0 ; v = 0.$$

- Source term specified by the **predicted flow rate**  $Q$  centered at rush hour:  $t = 0.5\text{h}$ .

- Transition to non-dimensional variables:

- $$t/\tau ; x/\lambda ; v \tau/\lambda ; \rho \lambda ; Q\tau$$

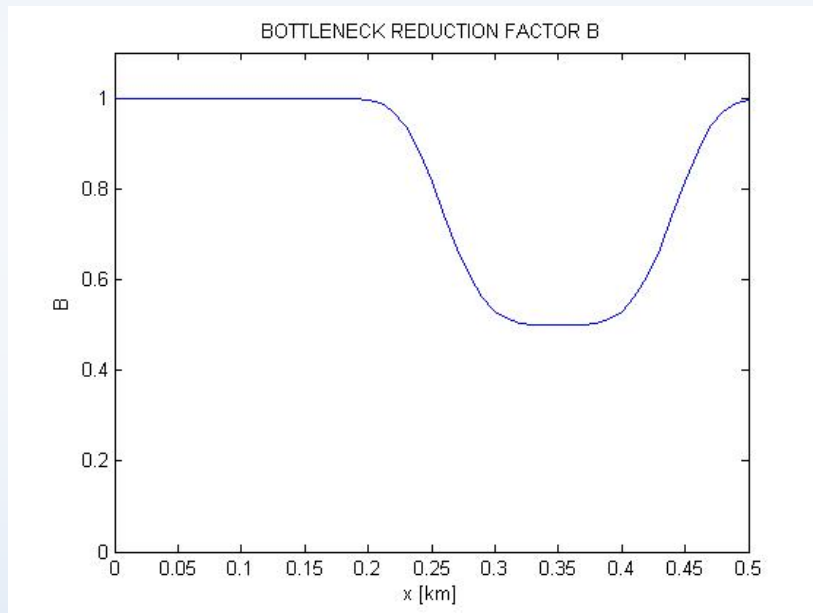
Macro-modeling based on fundamental diagram of flow and continuity equation.

Boundary condition is determined by the predicted flow.



# Example of the disturbed region

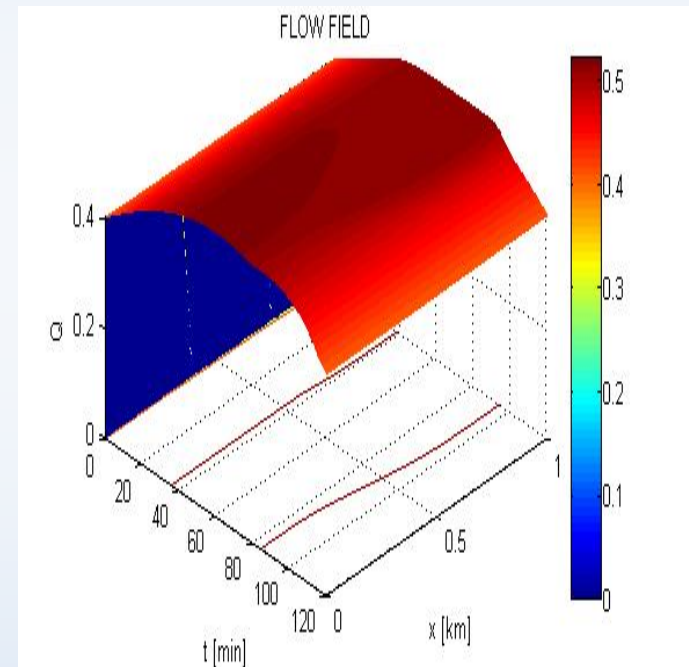
- Position:  $0.2\text{km} < x < 0.4\text{km}$
- Reduced speed:  $0.5 v_0$



Dependence of the velocity reduction factor  $B$  on  $x$ .

## Field distributions

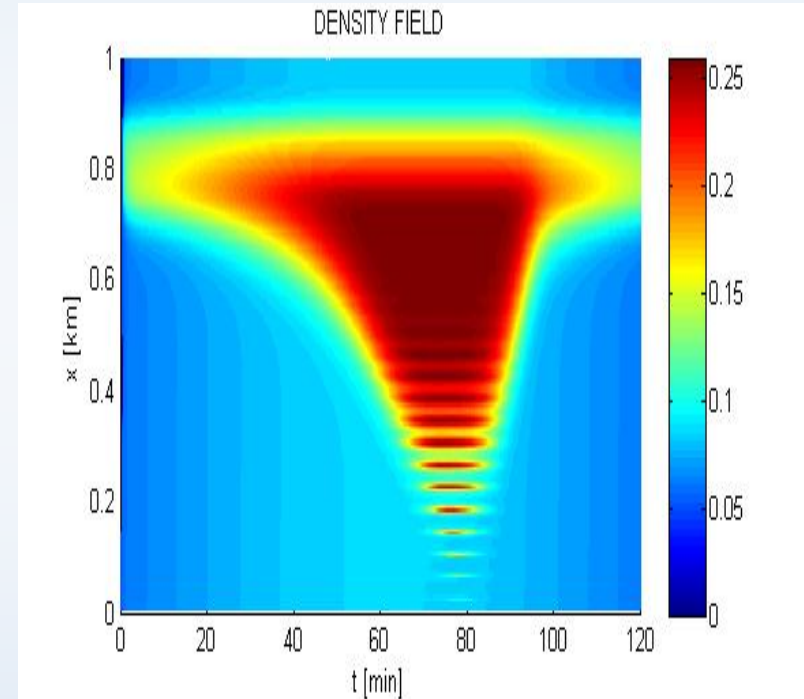
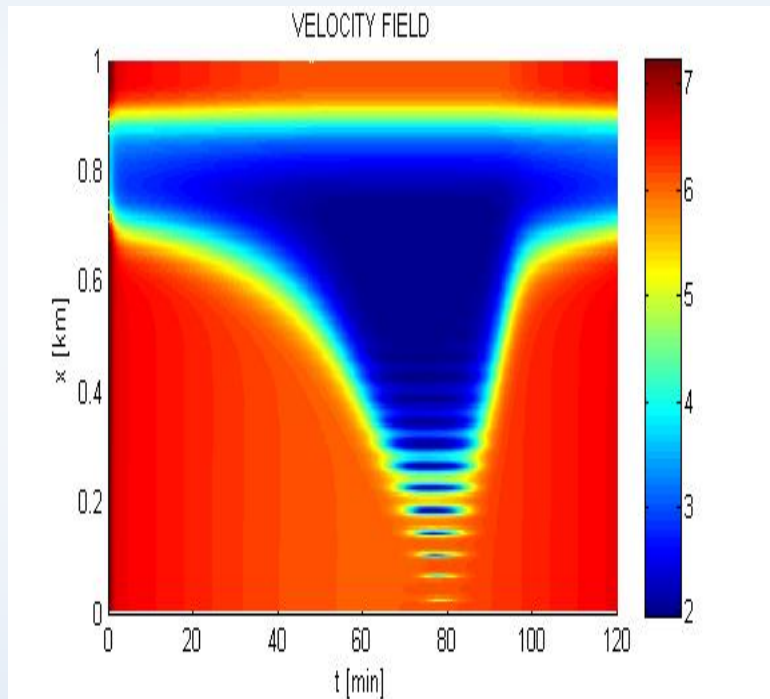
Traffic flow field



Parameters:  $v_0=130$  km/h ;  $Q_{max}=1875$  veh/h

# Example of the disturbed region

## Field distributions



Parameters:  $v_0=130$  km/h ;  $Q_{max}=1875$  veh/h







# Coclusions

- Information on traffic jams is vital for road users.
- Forecasting of traffic jams provides support for traffic information center and road services.
- We have shown that in spite of rather complex, non-linear, and stochastic character of traffic flow, it is possible to model the evolution of traffic jam at a disturbed region based upon the forecasted input flow and the proper speed limit that corresponds to driving conditions in severe weather.
- The next step is to transfer predicted data directly to drivers (e.g. over mobile phones).



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# References

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- I. Grabec, F. Švegl, *Modeling and Forecasting of Traffic Flow*, ISEP 2010, Ljubljana, SI
- F. Švegl, I. Grabec, *Prediction of winter driving conditions*, Proc. **SIRWEC – 15<sup>th</sup>**, Quebec, CA, 2010
- I. Grabec, F. Švegl, *Forecasting of traffic flow at a high-way bottleneck*, Proc. ISEP 2011, Ljubljana, SI
- This research was supported by the agencies *DRSC* and *DARS*, as well as EU projects: *Roadidea*, *iCAR* and EraSme: *Motrac*





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# Thank you for your attention!

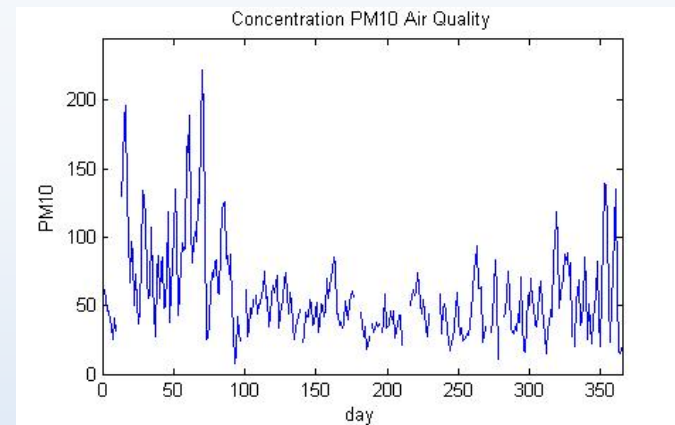
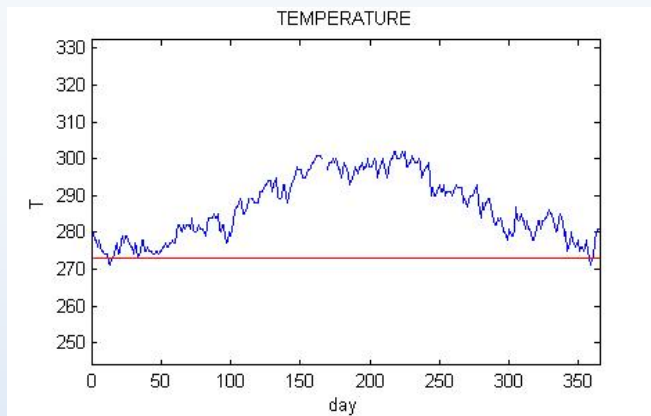
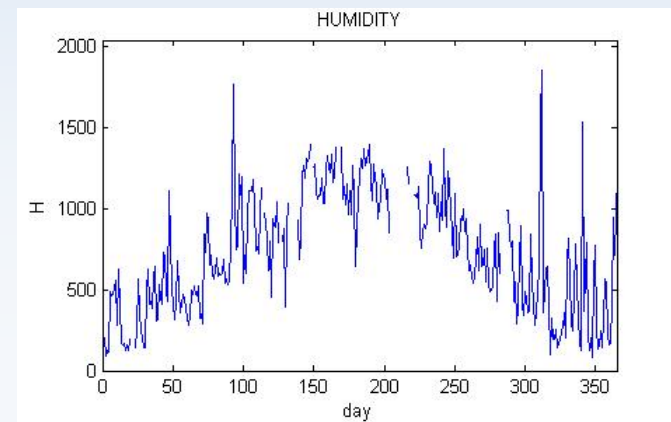
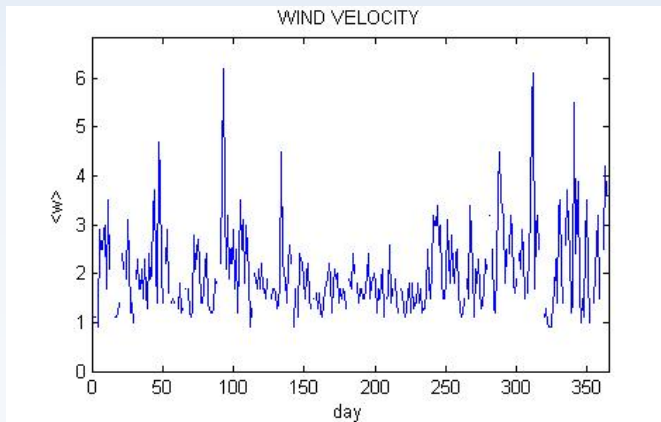
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# Kiitos mielenkiinnosta!





# Variables used in PM10 modeling





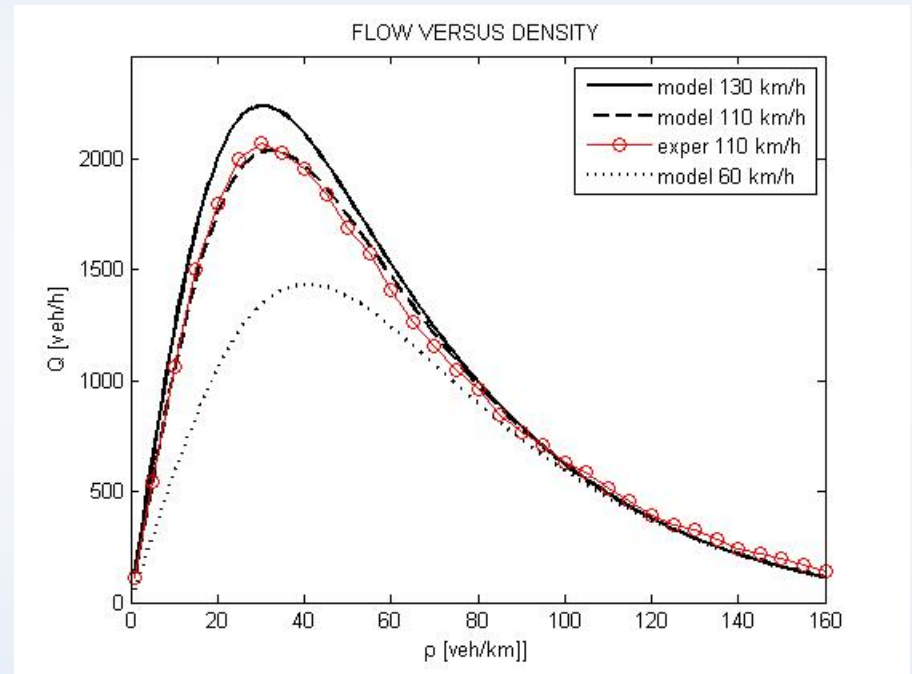
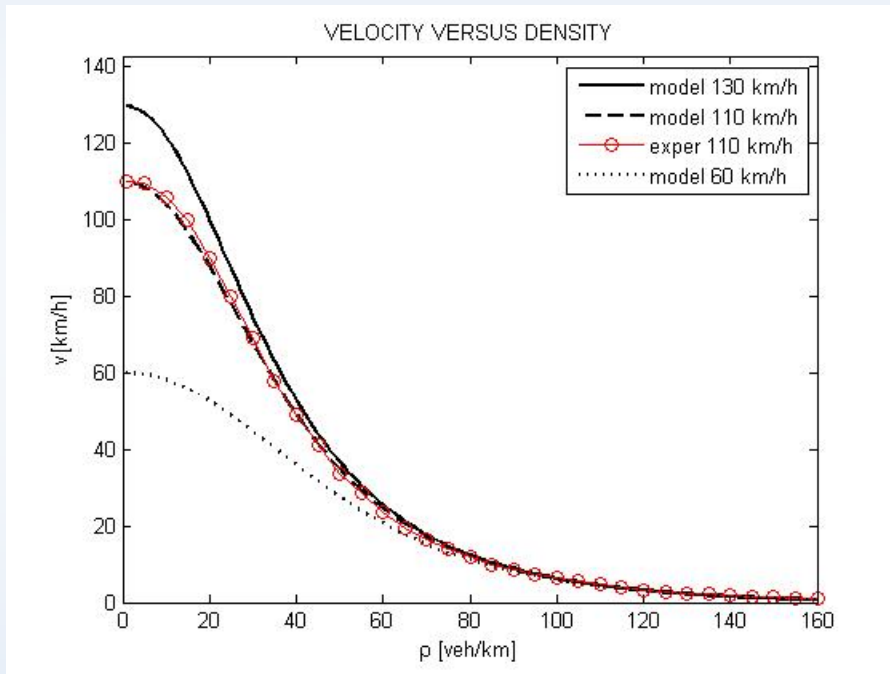
# Statistical variables

- **Basic variables:**
  - $r$  : distance between cars,  $\rho=1/r$  : density of cars
  - $v$  : mean velocity,
  - $ve(\rho)$  : equilibrium velocity
  - $Q=\rho v$  : flow rate
- **Parameters and reference variables:**
  - $\lambda \sim 5\text{m}$  : car length,  $r - \lambda$  : clear spacing
  - $\tau \sim 1\text{s}$  : reaction time
  - $u = C \lambda / \tau$  : characteristic velocity;  $C \sim 3$
  - $r = \lambda + \tau w$  : proper distance
  - $w = (r - \lambda) / \tau$  : proper velocity





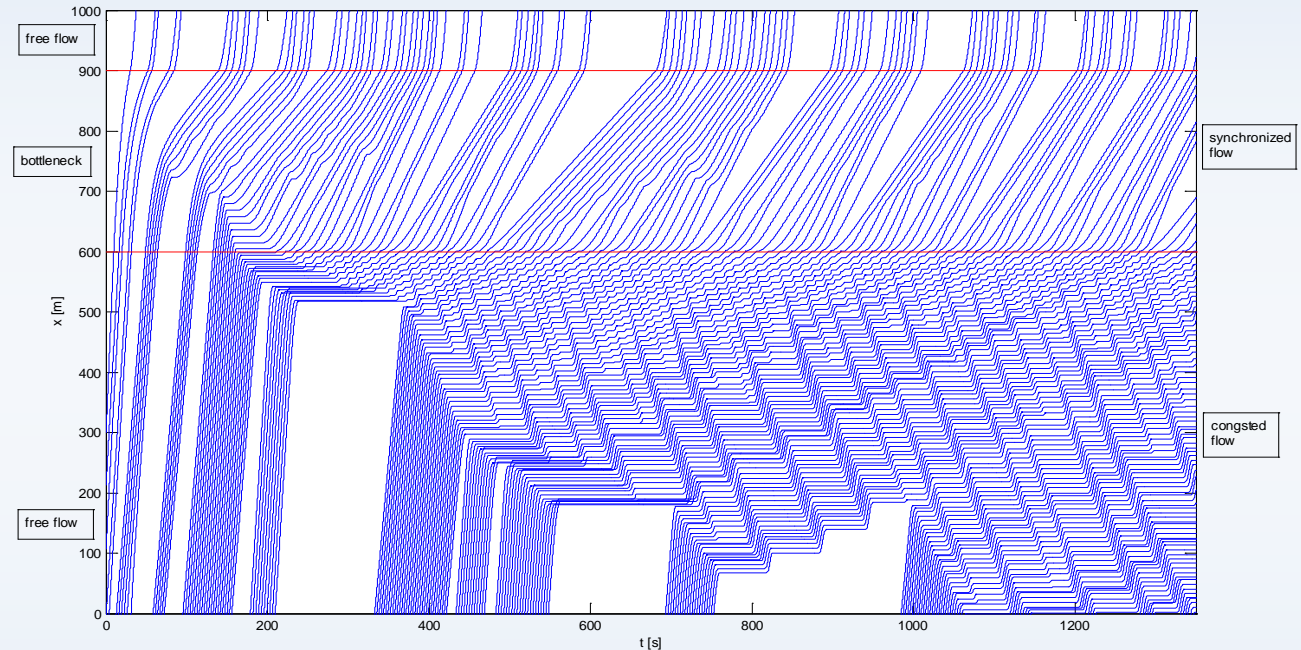
# Fundamental diagram of traffic



# Micro-dynamic modeling of traffic jam evolution

Micro-dynamic model stems from driving rules and predictor of traffic flow.

Micro-model is not convenient for application.



The goal: Macro-modeling based on fundamental diagram of flow and continuity equation. Boundary condition is determined by the predicted flow

